



# Image Space Tensor Field Visualization using a LIC-like Method

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# Outline

## 1 Introduction

Focus

Tensor field visualization

Motivation and Goals

## 2 The method

Step 0: Input

Step 1: Projection to Image Space

Step 2: Silhouette detection

Step 3: Advection

Step 4: Compositing

## 3 Results

## 4 Problems and Further Work



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# Focusing on ...

- Second-order tensor fields
- Diffusion tensors
  - positive definite
  - symmetric
  - three orthogonal eigenvectors without orientation
- Medical DTI visualization, but not limited to



# Tensor field visualization

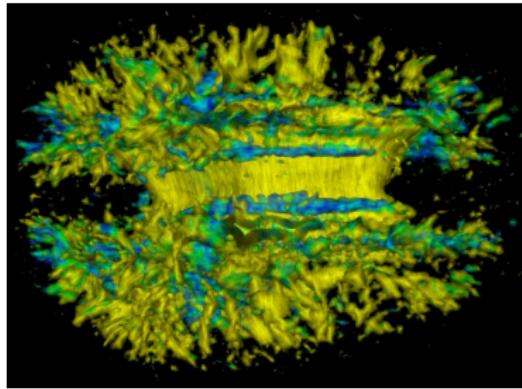
- Inspired by methods used in Scalar- and Vector field visualization
- Often using derived metrics
- Common methods:
  - Colormaps
  - HyperLIC (Zheng et al. [ZP03])
  - Tensor Glyphs (Kindlmann [Kin04])
  - Direct Volume Rendering (foundations in [Bli82, KVH84])
  - Advection Diffusion Tensorlines (Kindlmann et al. [WKL99])
  - Hyperstreamlines (Delmarcelle et al. [DH92])



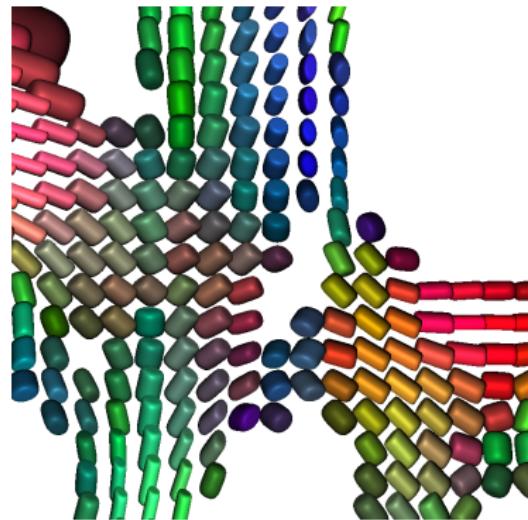
# Weaknesses and Problems

- Limitation to local or global data representation
  - no smooth and interactive transition between levels of detail
- Severe limitations in data size
- Interactive performance
- Limitations in number of represented tensor attributes

# Examples I



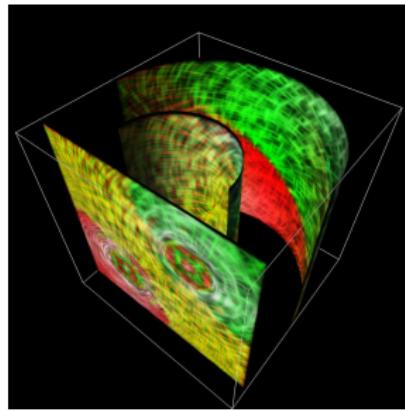
(a) HyperLIC



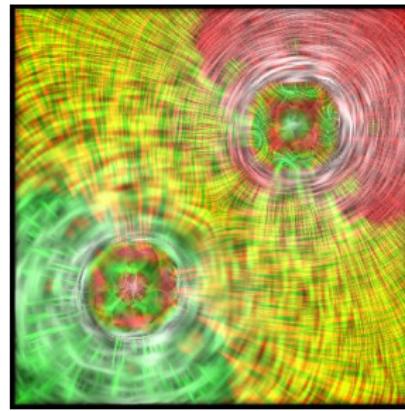
(b) Superquadrics

**Figure:** HyperLIC and Superquadric Tensor Glyphs

## Examples II



(a) Method applied to several surfaces



(b) XZ-Slice

**Figure:** Hotz et al. [HFHJ09]. Limitation to type of surface.



# Motivation and Goals

- Easy perceptibility of structures
  - More bold representation of diffusion structures
- Continuous perception of structures during transformation
  - Often problematic with image space based methods
- Allow smooth transition between local and global structures
- Realtime ability
- Applicability on arbitrary geometry



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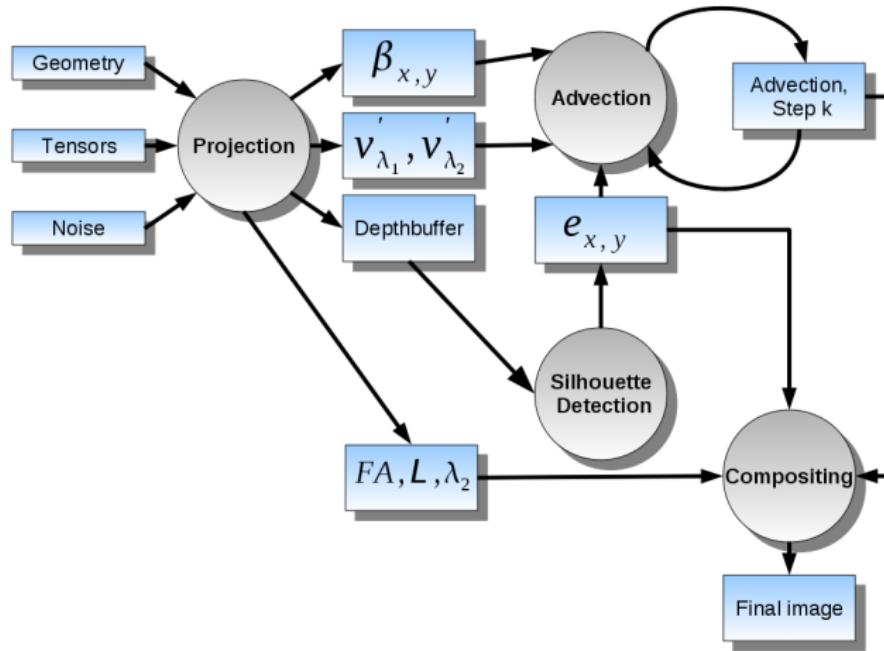
## 4 Problems and Further Work



# Overview I

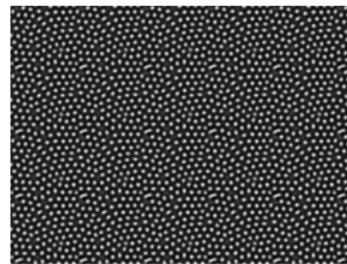
- Move problem to image space
- Divide into small parallelizable parts
  - Utilize GPU parallelism
- Implementation using OpenGL, GLSL and Framebuffer Objects
  - But smaller float precision
  - Many limitations
- Textures as transport media

# Overview II





# Noise



**Figure:** Tiled 100x100 pixel reaction diffusion texture with  $D_a = 0.125$  and  $D_b = 0.031$ .

- Initial calculation of input noise
  - Reaction Diffusion ([Tur52])
  - Create once, reuse every pass
- Since computational expensive: tiling

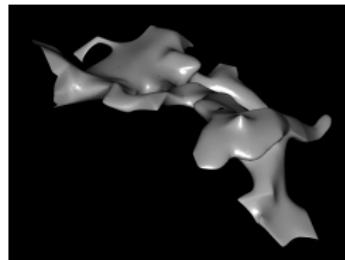
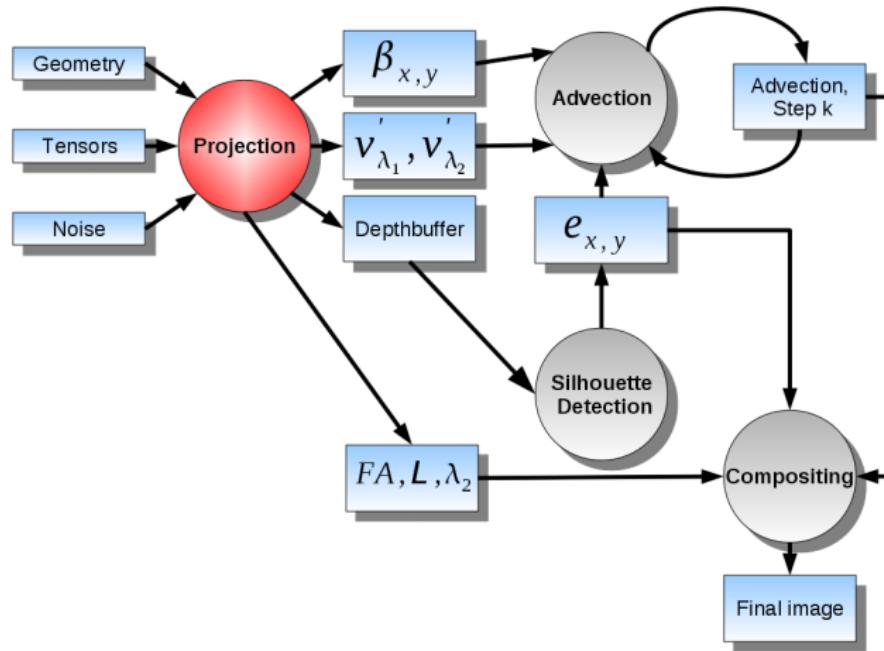


Figure: Input geometry with Phong lighting.

- Geometry calculated using arbitrary metric and algorithm
- Tensors uploaded as two 3D texture coordinates
- Requirements to geometry:
  - Smooth normals
  - Not self-intersecting

# Step 1: Projection to Image Space



# Tensor projection I

- Tensor interpolated using GPU
- Projection to geometry surface ( $n = s \cdot v_{\lambda_3}$ ):  
$$T' = P \cdot T \cdot P^T \text{ mit } P = \begin{pmatrix} 1 - n_x^2 & -n_y n_x & -n_z n_x \\ -n_x n_y & 1 - n_y^2 & -n_z n_y \\ -n_x n_z & -n_y n_z & 1 - n_z^2 \end{pmatrix}.$$
- Eigenvalue decomposition using Hasan et al. [HBPA01]
  - Eigenvalues:  $\lambda_i$  with  $i \in \{1, 2\}$
  - Eigenvectors:  $v_{\lambda_i}$  with  $i \in \{1, 2\}$
- Eigenvectors still in geometries object coordinate system



# Tensor projection II

- Projection to image space using OpenGL's Modelviewmatrix  $M_M$  and Projectionmatrix  $M_P$ :  
 $v'_{\lambda_i} = M_P \times M_M \times v_{\lambda_i}$ , with ( $i \in 1, 2$ ) and  $v'_{\lambda_i} \in \mathbb{R}^2$
- May not need to be orthogonal anymore ( $\langle v'_{\lambda_1}, v'_{\lambda_2} \rangle \neq 0$ )
- Scale to [0, 1]:  
 $v''_{\lambda_i} = \frac{1}{2} + \frac{1}{2} * \frac{v'_{\lambda_i}}{\|v'_{\lambda_i}\|_\infty}$  with  $i \in \{1, 2\}$  and  $\|v'_{\lambda_i}\|_\infty \neq 0$



# Noise Texture Mapping I

- To ensure consistency during transformation
- Many methods available
  - Texture Atlases ([PCK04, IOK00])
  - Reaction Diffusion directly on the geometry ([Tur91])
  - 3D textures ([WE04])
  - Mostly computational expensive or geometry dependent results
- Own heuristics developed
  - Not  $C^1$  constant
  - May introduce minor distortions
  - Allows seamless scaling
  - Good trade-off between computation time and visual quality



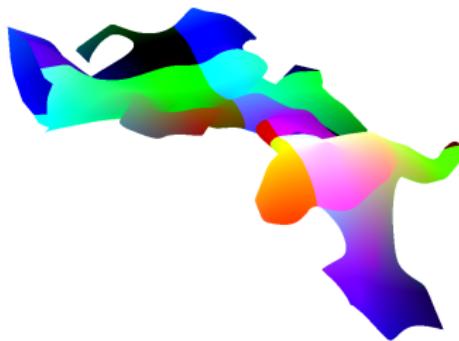
# Noise Texture Mapping II

- Transformation of vertex  $v_g$  to voxelized space:

$$v_{voxel} = v_g \cdot \begin{pmatrix} l & 0 & 0 & -b_{min_x} \\ 0 & l & 0 & -b_{min_y} \\ 0 & 0 & l & -b_{min_z} \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

- $l$  is its size,  $b_{min}$  origin of voxel space in world coordinates
- Discretize to voxels borders  $v_{hit} = v_{voxel} - \lfloor v_{voxel} \rfloor$
- Texture coordinate  $t$  is then defined as:  
 $t = (v_{hit_i}, v_{hit_j})$ , with  $i \neq j \neq k \wedge (n_k = \max\{n_i, n_j, n_k\})$

# Noise Texture Mapping III)

(a)  $v_{hit}$ (b)  $t$ 

**Figure:** Illustration of  $v_{hit}$  and  $t$  for illustration.

# Noise Texture Mapping IV



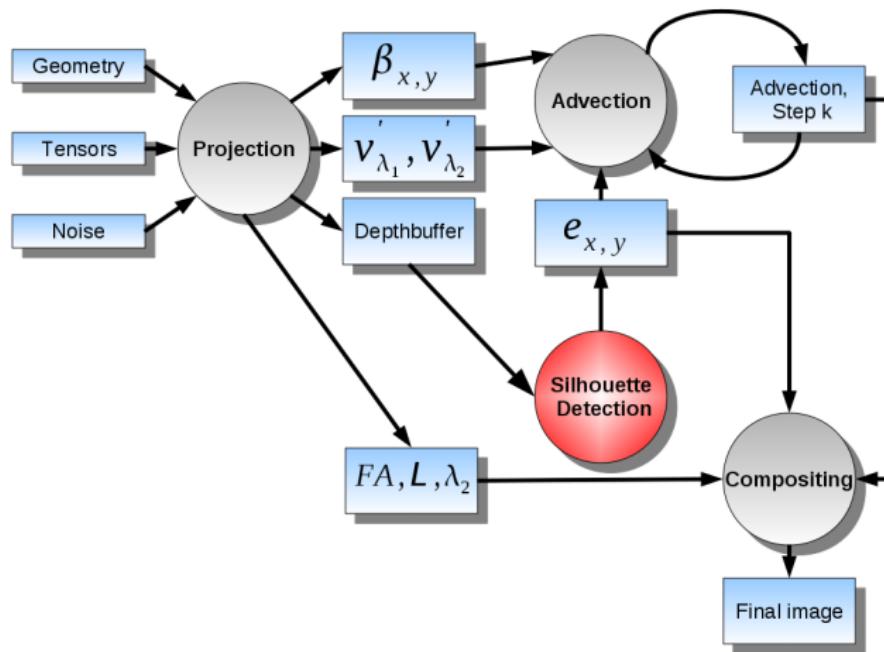
**Figure:** Noise mapped to surface ( $\beta_{i,j}$ ).



# Further calculations

- Phong intensity  $\mathcal{L}$
- Mean Diffusivity
- Fractional Anisotropy
- Colormapping:  $c^{FA \cdot v_{\lambda_i}}(T) = \frac{|v_{\lambda_i}|}{\|v_{\lambda_i}\|} * FA(T)$

# Step 2: Silhouette detection I

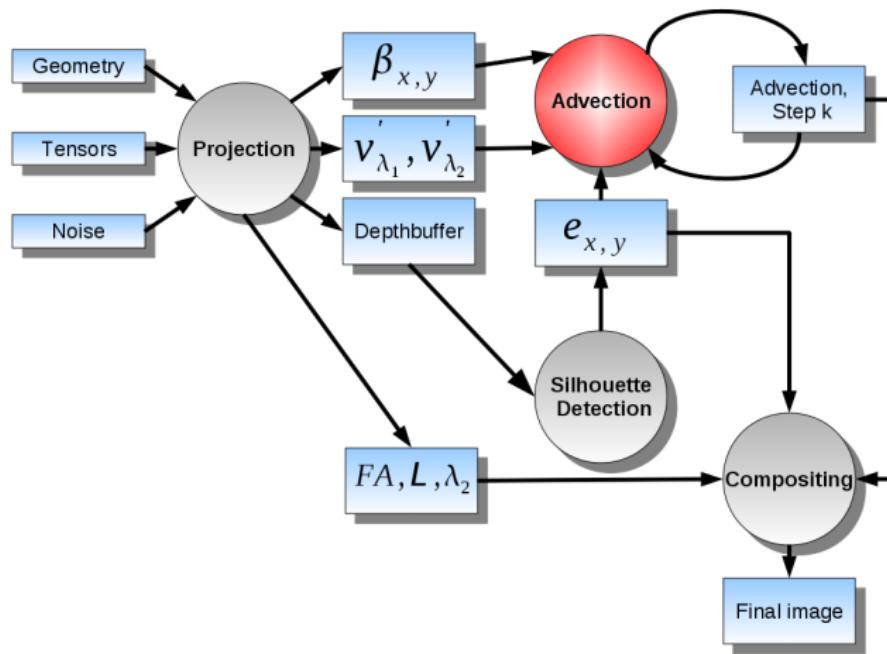




## Step 2: Silhouette detection II

- Creation of silhouette texture  
 $e : (x, y) \rightarrow s$ , with  $x, y, s \in [0, 1]$  using depthbuffer
- Fold using Laplace filter kernel:  $D_{xy}^2 = \begin{bmatrix} 0 & 1 & 0 \\ 1 & -4 & 1 \\ 0 & 1 & 0 \end{bmatrix}$

# Step 3: Advection I





## Step 3: Advection II

- Access to discrete, intermediate LIC-textures  $P^{\lambda_1}$  and  $P^{\lambda_2}$  using:  $f_P : (x, y) \rightarrow p$ , with  $x, y, p \in [0, 1]$ 
  - Interpolation
- Iteration on both textures for each pixel:

$$\forall x, y \in [0, 1] : \forall \lambda \in \{\lambda_1, \lambda_2\} :$$

$$p_0^\lambda = \beta_{x,y},$$

$$p_{i+1}^\lambda = k \cdot \beta_{x,y} + (1 - k) \cdot \frac{f_{p_i^\lambda}(x + v'_{\lambda_x}, y + v'_{\lambda_y}) + f_{p_i^\lambda}(x - v'_{\lambda_x}, y - v'_{\lambda_y})}{2}.$$

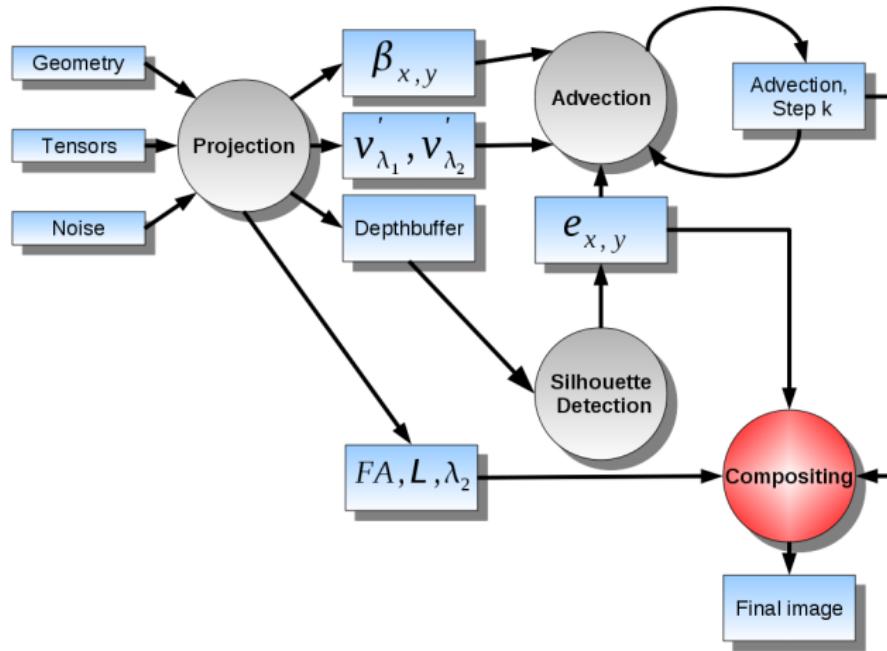
- $k$  describes "roughness" (the smaller  $k$  is, the more smooth the final image looks)
- Advection needs to be done in both directions, since eigenvectors do not have an orientation
- Stop iteration if  $|p_i^\lambda - p_{i+1}^\lambda| < \epsilon$

## Step 3: Advection III



Figure: Advection of Eigenvector field  $v'_{\lambda_1}$  after 10 iterations.

# Step 4: Compositing I





## Step 4: Compositing II

- Final step after  $i$  iterations
  - Possible to stretch advection iterations over multiple frames
- Clipping using MD, FA or another metric
- Set depthbuffer information
- Depth-enhancing ([CCG<sup>+</sup>08]) for better plasticity
- Very flexible
  - blend in colormaps



## Step 4: Compositing III

- Color for each pixel with advected textures  $P_i^{\lambda_1}$  and  $P_i^{\lambda_2}$ :

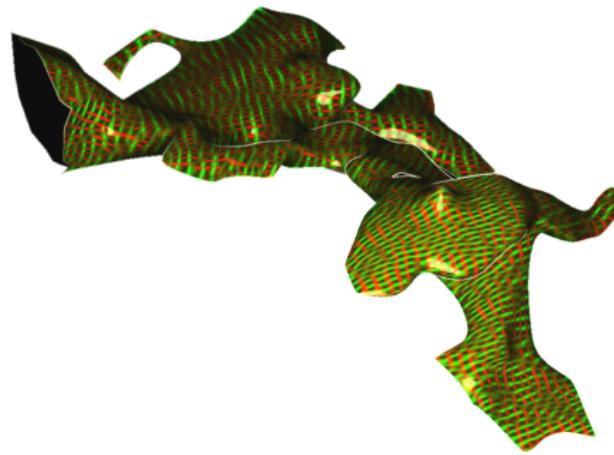
$$R = \frac{r \cdot f_{p_k^{\lambda_2}}(x, y)}{8 \cdot f_{p_k^{\lambda_1}}^2(x, y)} + e_{x,y} + \text{light}(\mathcal{L}_{x,y}),$$

$$G = \frac{(1 - r) \cdot f_{p_k^{\lambda_1}}(x, y)}{8 \cdot f_{p_k^{\lambda_2}}^2(x, y)} + e_{x,y} + \text{light}(\mathcal{L}_{x,y}), \text{ and}$$

$$B = e_{x,y} + \text{light}(\mathcal{L}_{x,y}).$$

- Silhouette texture:  $e$  and Light:  $\mathcal{L}$
- $r$  defines ratio between both eigenvector fields in the final image

## Step 4: Compositing IV



**Figure:** Composed image showing diffusion-directions through a fabric like structure.



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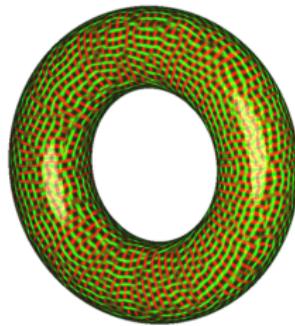
Step 2: Silhouette detection

Step 3: Advection

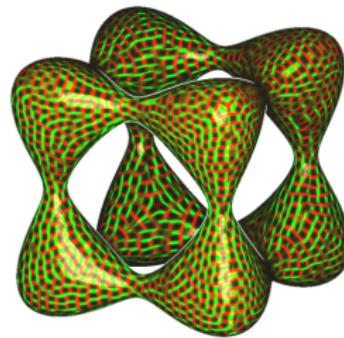
Step 4: Compositing

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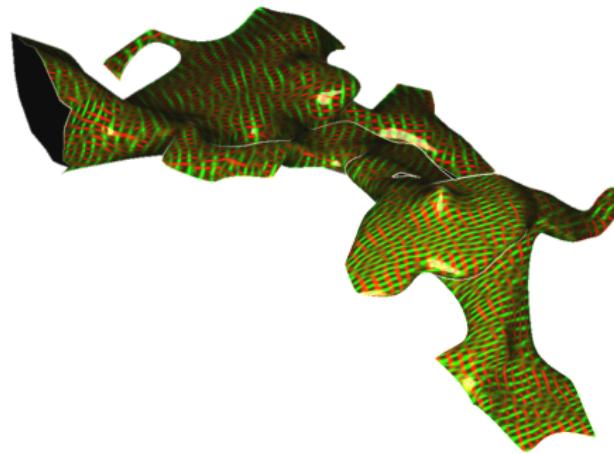
(a) Torus



(b) Tangle

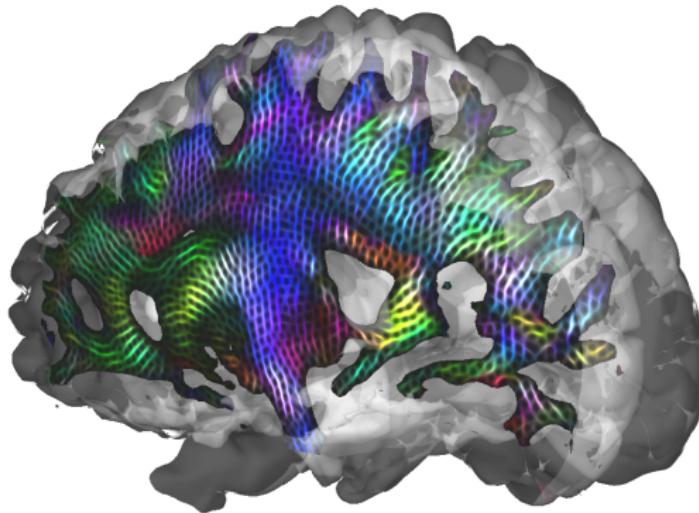
**Figure:** Implicit,  $C^1$  steady surfaces ([KHH<sup>+</sup>07])

# Small part of DTI dataset



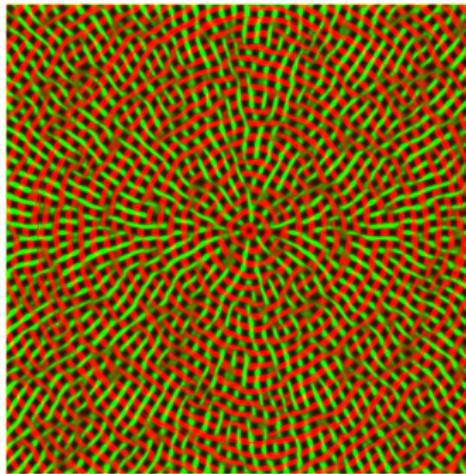
**Figure:** Small part of Corpus Callosum in a DTI dataset. (58624 triangles, 30 FPS (Geometry: 69%))

# Neural Fibers (DTI)



**Figure:** Diffusion along neural fibers (Anwander et al. [ASH<sup>+</sup>09]).  
(41472 Triangles, 32 FPS (Geometry: 72%))

# Single Point Load (Mechanics)



**Figure:** Single Point Load dataset.



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# Problems

- Noise texture mapping strongly dependent on quality of normals
- Minor blurring effects
- Lighting with Phong often not optimal for spatial perception of geometry



## Further Work

- Reduction of rendered geometry for further performance improvement
  - Since geometry rendering is lion's share in overall rendering time
- Extend to tensor fields of higher order
- Variation of spot sizes and density in initial noise texture
  - Corresponding to eigenvalues
  - As in [HFHJ09]



# Thank You for listening

## Questions?



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